## Behavioral/Systems/Cognitive

# Globally Altered Structural Brain Network Topology in Grapheme-Color Synesthesia

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Synesthesia is a perceptual phenomenon in which stimuli in one particular modality elicit a sensation within the same or another sensory modality (e.g., specific graphemes evoke the perception of particular colors). Grapheme-color synesthesia (GCS) has been proposed to arise from abnormal local cross-activation between grapheme and color areas because of their hyperconnectivity. Recently published studies did not confirm such a hyperconnectivity, although morphometric alterations were found in occipitotemporal, parietal, and frontal regions of synesthetes. We used magnetic resonance imaging surface-based morphometry and graph-theoretical network analyses to investigate the topology of structural brain networks in 24 synesthetes and 24 nonsynesthetes. Connectivity matrices were derived from region-wise cortical thickness correlations of 2366 different cortical parcellations across the whole cortex and from 154 more common brain divisions as well. Compared with nonsynesthetes, synesthetes revealed a globally altered structural network topology as reflected by reduced small-worldness, increased clustering, increased degree, and decreased betweenness centrality. Connectivity of the fusiform gyrus (FuG) and intraparietal sulcus (IPS) was changed as well. Hierarchical modularity analysis revealed increased intramodular and intermodular connectivity of the IPS in GCS. However, connectivity differences in the FuG and IPS showed a low specificity because of global changes. We provide first evidence that GCS is rooted in a reduced small-world network organization that is driven by increased clustering suggesting global hyperconnectivity within the synesthetes' brain. Connectivity alterations were widespread and not restricted to the FuG and IPS. Therefore, synesthetic experience might be only one phenotypic manifestation of the globally altered network architecture in GCS.

## Introduction

Synesthesia is a perceptual phenomenon in which stimuli in one modality elicit a sensation within the same or another sensory modality. Several different forms of synesthesia are known, the most investigated of which is grapheme-color synesthesia (GCS) (Rich et al., 2005; Simner et al., 2006). Grapheme-color synesthetes automatically perceive a particular color in association with a particular letter or digit.

Based on the findings of functional studies (Nunn et al., 2002; Rich and Mattingley, 2002; Hubbard et al., 2005a,b; Hubbard and Ramachandran, 2005; Weiss et al., 2005; Esterman et al., 2006; Sperling et al., 2006; Muggleton et al., 2007; Beeli et al., 2008), Hubbard and Ramachandran proposed an influential two-stage

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model for GCS (Hubbard and Ramachandran, 2005; Hubbard, 2007). First, synesthetic experience stems from abnormal cross-activation in the form of "hyperconnections" between the "grapheme" and "color" areas in the fusiform gyrus (FuG). Second, the two perceptions associated with the FuG are then bound together by top-down mechanisms supported by the parietal cortex, and resulting in "hyperbinding."

Recent structural imaging studies in GCS have used diffusion tensor imaging (Rouw and Scholte, 2007; Jäncke et al., 2009) and voxel-based (Weiss and Fink, 2009; Rouw and Scholte, 2010) and surface-based (Jäncke et al., 2009) morphometry. These studies have only been able to support this model in part, and only one study was able to confirm the involvement of the FuG and the parietal cortex (Weiss and Fink, 2009). The morphometric analysis of a single subject with interval–taste and tone– color synesthesia did support the idea of hyperconnectivity between brain areas subserving auditory and gustatory processing (Hänggi et al., 2008).

The present study applied a new approach to investigate the pattern of structural interconnections in the FuG, intraparietal sulcus (IPS) and across the entire cortex. Using magnetic resonance imaging (MRI) surface-based morphometry and graphtheoretical network analyses (Watts and Strogatz, 1998; Bullmore and Sporns, 2009), we investigated the topological characteristics of whole cortical anatomical networks in 24 grapheme-color syn-

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esthetes and 24 nonsynesthetes. There is mounting evidence that cortical thickness covariations are an indicator of connectivity (Mechelli et al., 2005; Worsley et al., 2005; Lerch et al., 2006). Recently, graph-theoretical network analyses based on cortical thickness correlations and white matter tractography were used to investigate brain network characteristics in healthy (He et al., 2007; Chen et al., 2008; Hagmann et al., 2008; Gong et al., 2009; Honey et al., 2009) and clinical (He et al., 2008, 2009) samples. Based on surface-based morphometry, the connectivity matrices in the present study were derived from region-wise cortical thickness correlations between 2366 anatomical parcellations and between 154 more common anatomical regions and subjected to network analyses. We investigated weighted network characteristics including the clustering coefficient, path length, smallworld indices, degree, and betweenness centrality as well as modularity. We expected that hyperconnectivity is either local, in case the two-stage model is valid, or even more global and not restricted to local anatomical differences as suggested by others (Bargary and Mitchell, 2008).

## Materials and Methods

#### Subjects

Twenty-four synesthetes (20 females) with a mean age of 29.2 years (SD  $\pm$  10.1 years) and 24 nonsynesthetes (20 females) matched for age (27.3  $\pm$  6.2 years), sex, handedness, and education participated in the study. Given that most of the participants in both groups had an academic background, their years of education were closely matched. All subjects had already participated in one of our previous investigations (Jäncke et al., 2009). Synesthetes reported a lifelong history of grapheme-color perception (i.e., as long as they could remember) and were tested for their color perception to letters and numbers with the established "test of genuineness" that is typically used for the evaluation of synesthesia (Baron-Cohen et al., 1987). All synesthetes had to repeat this test at least 1 month later, all demonstrating constant synesthetic perception. All participants were consistently righthanded according to the procedure proposed by Annett (1970); had no history of neurological, neuropsychological, or psychiatric disease; and reported no use of drugs or medication. The local ethics committee approved the study, and written informed consent was obtained from all participants.

#### MRI data acquisition

MRI scans were acquired using a 3.0T Philips Intera whole-body scanner (Philips Medical Systems) equipped with a transmit–receive body coil and a commercial eight-element sensitivity encoding (SENSE) head coil array. A volumetric three-dimensional (3D) T1-weighted gradient echo sequence (turbo field echo) scan was obtained from all 48 participants with a spatial resolution of  $0.86 \times 0.86 \times 0.75$  mm (matrix,  $256 \times 256$  pixels; 180 slices). Additional imaging parameters were as follows: field of view,  $220 \times 220$  mm; echo time, 2.3 ms; repetition time, 20 ms; flip angle,  $20^{\circ}$ .

#### Surface-based morphometry

Cortical surface reconstruction and volumetric segmentation was performed with the FreeSurfer image analysis suite (version 4.0.3), which is documented and freely available for download on-line (http://surfer. nmr.mgh.harvard.edu/). The technical details of these procedures were described in previous publications (Dale et al., 1999; Fischl et al., 1999a,b, 2001, 2002, 2004a,b; Fischl and Dale, 2000; Ségonne et al., 2004). Briefly, the 3D structural T1-weighted MRI scan was used to construct models of each subject's cortical surface to measure brain features such as cortical thickness, cortical surface area, and cortical volume. This is a fully automated procedure involving segmentation of the cortical white matter (Dale et al., 1999), tessellation of the gray/white matter junction, inflation of the folded surface tessellation patterns (Fischl et al., 1999a), and automatic correction of topological defects in the resulting manifold (Fischl et al., 2001). This surface was then used as the starting point for a deformable surface algorithm designed to find the gray/white and pial (gray matter/CSF) surfaces with submillimeter precision (Fischl and Dale, 2000). The procedures for measuring cortical thickness have been validated against histological analysis (Rosas et al., 2002) and manual measurements (Kuperberg et al., 2003; Salat et al., 2004). This method uses both intensity and continuity information from the surfaces in the deformation procedure to interpolate surface locations for regions in which the magnetic resonance image is ambiguous (Fischl and Dale, 2000). For each subject, cortical thickness of the cortical ribbon was computed on a uniform grid (comprised by vertices) with 1 mm spacing across both cortical hemispheres, with the thickness defined by the shortest distance between the gray/white and pial surface models. The thickness maps produced are not limited to the voxel resolution of the image and are thus sensitive for submillimeter differences between groups (Fischl and Dale, 2000). Thickness measures were mapped to the inflated surface of each participant's brain reconstruction, allowing visualization of data across the entire cortical surface (i.e., gyri and sulci) without the data being obscured by cortical folding. Each subject's reconstructed brain was then morphed to an average spherical surface representation that optimally aligned sulcal and gyral features across subjects (Fischl et al., 1999b). This procedure provides accurate matching of morphologically homologous cortical locations among participants on the basis of each individual's anatomy while minimizing metric distortions. This transform was used to map the thickness measurements onto a common spherical coordinate system. In addition, the cerebral cortex was parcellated into units based on gyral and sulcal structure (Fischl et al., 2004b; Desikan et al., 2006), and a variety of surface-based data, including maps of cortical volume and surface area as well as curvature and sulcal depth, was created. Data were resampled for all subjects onto a common spherical coordinate system (Fischl et al., 1999b).

#### Graph-theoretical network analysis

Network (graph) construction. One of FreeSurfer's implemented parcellation schemes (aparc.a2005s) was used to compute mean cortical thickness in 154 anatomical structures across both cortical hemispheres (supplemental Fig. S1 and Table S2, available at www.jneurosci.org as supplemental material). These parcellations were used to construct the association (connectivity) matrix ( $A_{ij}$ ) based on the cortical thickness correlation matrix ( $C_{ij}$ ) between all pairs of parcellations, resulting in a  $154 \times 154$  association matrix (network) for the synesthetes and one for the nonsynesthetes (supplemental Fig. S1, available at www.jneurosci. org as supplemental material). These networks are referred to here as whole cortical 154-node networks, and they were used to investigate connectivity across both entire cortical hemispheres. A list of the anatomical labels of the nodes in the whole cortical 154-node network is presented in supplemental Table S2 (available at www.jneurosci.org as supplemental material).

Connectivity within a particular brain structure such as the FuG or IPS cannot be investigated within the whole cortical 154-node network because the FuG and IPS of one hemisphere is represented only as one node each in that network. Therefore, we constructed a much finer parcellated network to investigate connectivity across cortices in more detail as well as within the FuG and IPS. To this end, the cortical surface model of FreeSurfer's surface template (fsaverage), onto which the individual surface models of the synesthetes and nonsynesthetes were spatially registered, was parcellated into 100-mm<sup>2</sup>-sized, strip-like-shaped 2366 cortical regions across both hemispheres (1187 and 1179 parcellations in the left and right hemisphere, respectively). The stripes were then reprojected onto each individual surface using the inverse transformations, and cortical thickness within each strip was measured by averaging across all vertices located within a particular strip. These 2366 parcellations were used to construct the association matrix  $(A_{ii})$  based on the cortical thickness correlation matrix  $(C_{ii})$  between all pairs of stripes, resulting in two 2366  $\times$  2366 association matrices (networks), one for the synesthetes and one for the nonsynesthetes (Fig. 1). These networks are referred to here as whole cortical 2366-node networks and were constructed to investigate connectivity across both hemispheres as well as within the FuG and IPS.

In addition, we investigated the connectivity of the FuG and its immediate neighboring areas in isolation from the rest of the brain. For this purpose, the whole cortex was divided into 2053 triangular parcellations, from which 66 nodes (parcellations) per hemisphere were selected that together comprise the fusiformlingual network (supplemental Fig. S2, available at www.jneurosci.org as supplemental material). These nodes were located within the FuG, lingual gyrus, lingual sulcus, anterior and posterior part of the collateral transverse sulcus, lateral occipito-temporal sulcus, inferior occipital gyrus and sulcus, and the calcarine cortex. The calcarine cortex is not directly adjacent to the fusiform cortex but was included in this network because of our previous findings of changed cortical thickness in synesthetes in that visual region (Jäncke et al., 2009). These triangular parcellations were used to construct the fusiform-lingual association matrix  $(A_{ii})$  based on the cortical thickness correlation matrix  $(C_{ij})$  between all pairs of triangles, resulting in two  $132 \times 132$  association matrices, one for the synesthetes and one for the nonsynesthetes (supplemental Fig. S2, available at www.jneurosci.org as supplemental material). The left FuG was parcellated into 18 nodes, and the right FuG was parcellated into 17 nodes. These networks are referred to here as fusiform-lingual 132-node networks and were constructed to investigate connectivity within the fusiform-lingual complex and its adjacent areas in isolation from all other cortical areas of the brain.

To rule out any influence of the node's shape (stripes vs triangles), we also investigated a high-resolution whole cortical 2053-node network derived from triangular-shaped parcellations (supplemental Fig. S2*C*, available at www.jneurosci.org as supplemental material). Network measurements of this whole cortical 2053-node network derived from triangularshaped parcellations (results not shown) is very similar to the network measurements of the whole cortical 2366-node network derived from strip-shaped parcellations (see supplemental Discussion, available at www.jneurosci.org as supplemental material).

*Threshold selection.* Networks (graphs)  $G_r$  were represented by weighted matrices  $(A_{ij})$ , one matrix for each correlation threshold r)

with *N* nodes and  $K_r$  edges, where nodes represent cortical regions and edges represent the weighted connections between these cortical regions. There is currently no definitive and generally accepted strategy for applying a particular threshold. Each connectivity matrix was therefore thresholded repeatedly over a wide range of correlation thresholds in increments of r = 0.025 from r = 0.15 to r = 0.525, resulting in 16 networks with different connection densities per group. The fusiform-lingual 132-node network was thresholded only up to r = 0.50 because at a correlation threshold of r = 0.525, several nodes would become disconnected from the network.

network construction.

This kind of thresholding resulted in different number of edges between the networks of the groups because of differences in their interregional cortical thickness correlations (see Fig. 1 and supplemental Fig. S1, available at www.jneurosci.org as supplemental material). Thus, between-group differences in network characteristics might also reflect changes in wiring costs and not only alterations in the topological organization of the network (Achard and Bullmore, 2007; Stam et al., 2007). To control for this wiring cost effect, we also thresholded the correlation matrix  $(C_{ij})$  of the whole cortical 154-node and the fusiform-lingual 132-node networks of each group into matrices with fixed sparsities (percentages of edges by using relative correlation thresholds). Only results of the absolute thresholds are discussed here, but our sparsity analyses revealed that the network measures are not affected by these differing wiring costs (see supplemental Discussion, available at www. jneurosci.org as supplemental material).

*Small-world analysis.* The network analysis software tnet was used to analyze the networks (Opsahl et al., 2008; Opsahl, 2009; Opsahl and Panzarasa, 2009). tnet allows analyzing weighted networks (http://opsahl. co.uk/tnet/). The networks were analyzed according to the theory of small-world networks as introduced by Watts and Strogatz (1998; Bullmore and Sporns, 2009). To make our network parameters comparable with those parameters obtained in similar studies that used cortical thickness correlations, we followed their procedures as closely as possible (He et al., 2007, 2008, 2009; Chen et al., 2008; Gong et al., 2009).



row) and 2366-node (middle row) network nodes and the connectivity matrices (cortical thickness correlations) of the

synesthetes (bottom row left) and nonsynesthetes (bottom row right), representing the undirected weighted edges

of the whole cortical 2366-node networks, are shown. The connectivity matrices of the whole cortical 154-node networks

of the two groups are shown in supplemental Figure S1 (available at www.ineurosci.org as supplemental material). Note

that the black and greyish parcellations seen on the medial surfaces represent the medial wall and were not included for the

Coarse parcellation scheme

(right hemisphere, lateral view)

**Coarse parcellation scheme** 

(left hemisphere, medial view)

Small-world indices were derived from the comparison of the real network with 100 random network realizations comprising the same number of nodes, edges, mean degree, and degree distribution. For the densest whole cortical 2366-node networks, <100 random networks were computed because of the enormous computational resources needed for constructing these random networks. However, this is not a problem because measurement variances are almost zero for such dense random networks. The procedure for constructing the random networks was described in more detail previously (Opsahl et al., 2008).

On the basis of these structural brain networks, key characteristics that describe the overall architecture of a network were computed, including the clustering coefficient  $C_r$  and the characteristic path length  $L_r$  (Watts and Strogatz, 1998). In binary networks, the  $C_r$  is the ratio between the number of connections between the direct neighbors of a node and the total number of possible connections between these neighbors and provides information about the level of local connectedness within a network. The characteristic  $L_r$  of a binary network gives the average number of connections that have to be crossed to travel from each node to every other node in the network and provides information about the level of global communication efficiency of a network (van den Heuvel et al., 2009). The definitions of  $C_r$  and  $L_r$  in weighted networks, as implemented in tnet (http://opsahl.co.uk/tnet/), are based on the sum of the weights, and these formulas were reported previously (Opsahl et al., 2008; Opsahl, 2009; Opsahl and Panzarasa, 2009).

Networks with small-world organization have a  $C_r$  that is higher than the  $C_r$  of a comparable random, organized network ( $C_r$  random), while still having a short characteristic  $L_r$  similar in length to that of an equivalent random network ( $L_r$  random). Formally, small-world networks show a ratio  $\gamma_r$ , defined as  $C_r$  real/ $C_r$  random of  $\gg 1$ , and a ratio  $\lambda_r$ , defined as  $L_r$  real/ $L_r$  random of  $\sim 1$  (Watts and Strogatz, 1998; Sporns et al., 2004; Humphries et al., 2006; Humphries and Gurney, 2008). A high  $\gamma_r$  reflects a high level of local neighborhood clustering within a network, and a short normalized travel distance  $\lambda_r$  expresses a high level of global communication efficiency within a network (Watts and Strogatz, 1998; Sporns et al., 2004; Bullmore and Sporns, 2009).

Nodal centrality analysis. Hub regions were evaluated by weighted degree and betweenness centrality measures that were originally proposed for binary networks by Freeman (1978). Degree in weighted networks is taken as the sum of weights and labeled node strength (Barrat et al., 2004; Newman, 2004). The formula of this measure for weighted networks was described in more detail previously (Opsahl et al., 2008; Opsahl, 2009; Opsahl and Panzarasa, 2009). Centrality of a node expresses its structural or functional importance. Highly central nodes may serve as way stations for network traffic (betweenness centrality) or as centers for information integration (degree centrality). Degree centrality is the sum of weights incident upon a node (i.e., the sum of weights of the edges that a node has). Degree is often interpreted in terms of the capability of a node to catch whatever is flowing through the network. Betweenness centrality relies on the calculation of shortest distances in the network (Wasserman and Faust, 1994). Nodes that occur on many shortest paths (geodesics) between other nodes have higher betweenness centrality than those that do not. A node with high betweenness centrality is interpreted as a gatekeeper that is able to control the information flow through the node. We focused on the nodes representing both FuG and IPS because of the proposed roles of these structures in the genesis of GCS (Hubbard and Ramachandran, 2005; Hubbard, 2007; Weiss and Fink, 2009). We used Pajek software (http://vlado.fmf. uni-lj.si/pub/networks/pajek/) to visualize weighted, averaged (across all networks) degree and betweenness centrality scores of the nodes in the networks of the synesthetes and nonsynesthetes. Note that degree and betweenness centrality measures of the fusiformlingual 132-node network based only on connections among areas used to construct that fusiform-lingual network [see above, Network (graph) construction] and excluded the connections to all other cortical areas outside the fusiform-lingual complex.

*Modularity analysis.* Modularity analyses aim at detecting community structures (modules) within networks by using decompositions such as

hierarchical clustering. Many complex networks consist of a number of modules. Each module contains several densely interconnected nodes, and there are relatively few connections between nodes in different modules. Hubs can therefore be described in terms of their roles in this community structure (Bullmore and Sporns, 2009). To further characterize the nodes in the FuG and IPS in terms of intramodular (normalized within module degree) versus intermodular (participation coefficient) connectivity, we applied a hierarchical modularity analysis using the recently published Louvain algorithm (Meunier et al., 2009). Hierarchical modularity analysis was applied to each differently thresholded network of the whole cortical 2366-node and 154-node networks. The modularity measures (Q values) were averaged across all networks of a group, and the intramodular and intermodular connectivity measures were averaged across all networks of a group and across all FuG and IPS nodes in the case of the whole cortical 2366-node network. Note that, independent from the intrinsic connectivity architecture, a sparse connectivity and a higher number of modules goes with larger Q values.

Statistical analysis. For the statistical comparisons of global cortical thickness, volume, and surface area, we used analysis of covariance, controlling for intracranial volume. For the variables age and intracranial volume, as well as for the small-world parameter, centrality, and modularity measurements, we used *t* tests for independent samples. Error probability was set to p < 0.05 (two-tailed hypothesis testing, if not stated otherwise) for a single comparison, and Bonferroni correction was applied in analyses in which multiple comparisons occurred.

## Results

Age and global brain tissue characteristics are summarized in supplemental Table S1 (available at www.jneurosci.org as supplemental material). Right global cortical volume and left and right global cortical surface areas were increased in synesthetes compared with nonsynesthetes (corrected for intracranial volume), but these effects did not survive Bonferroni correction for multiple comparisons (corrected p = 0.05/7 = 0.007) and therefore will not be discussed further. There were no significant global mean cortical thickness differences between the groups. Thus, it was not necessary to correct for global cortical thickness.

#### Whole cortical 154-node and 2366-node network analysis

For reasons of completeness and comparability of the network parameters derived from the whole cortical 2366-node network with those derived from the 154-node network, we descriptively report also some differences in small-world parameters for the 2366-node network that were statistically not significant (see below). However, it is important to note that the effects reported in this study were consistently found in both the whole cortical 2366-node and the 154-node network analysis, but the error probabilities of these effects differed between the two network analyses.

In the absolute correlation threshold condition, the densest whole cortical 154-node network of the synesthetes comprised 6169 edges (connection density, 0.524), and the sparsest network comprised 764 edges (density, 0.067). In nonsynesthetes, the densest whole cortical network comprised of 5217 edges (density, 0.443), and the sparsest network comprised 399 edges (density, 0.034). These networks correspond to absolute correlation thresholds between r = 0.15 and r = 0.525. The connection densities of the whole cortical 154-node network were not statistically different between synesthetes and nonsynesthetes (mean/SD, 0.27/0.15 and 0.20/0.13; p = 0.18).

The densest whole cortical 2366-node network of the synesthetes comprised 1,066,127 edges (connection density, 0.381), and the sparsest network comprised 2468 edges (density, 0.00088). In non-

synesthetes, the densest whole cortical network comprised 923,552 edges (density, 0.330), and the sparsest network comprised 1,978 edges (density, 0.00071). These networks correspond to absolute correlation thresholds between r = 0.15 and r = 0.525. The connection densities of the whole cortical 2366-node network were not statistically different between synesthetes and nonsynesthetes (mean/SD, 0.15/0.12 and 0.12/0.10; p = 0.50).

### Small-world analysis

Across the whole range of absolute correlation thresholds of the whole cortical 154-node network, mean weighted clustering  $(C_r)$  of the synesthetes' networks was significantly increased (p = 0.001) compared with the mean weighted  $C_r$  of the nonsynesthetes' networks (Fig. 2A). The mean weighted path lengths  $(L_r)$  were significantly shorter (p = 0.001) in synesthetes compared with nonsynesthetes (Fig. 2B). In synesthetes, the small-world indices  $\gamma_r (C_r \text{ real}/C_r \text{ random})$  were significantly reduced (p = 0.011) across the whole range of correlation thresholds compared with nonsynesthetes (Fig. 2C). The small-world indices  $\lambda_r (L_r \text{ real}/L_r \text{ ran-}$ dom) were not significantly different (p = 0.17) between groups (Fig. 2D). In contrast, the classical small-world scalar parameter  $\sigma$  was significantly reduced (p = 0.003) in the networks of the synesthetes compared with the networks of the nonsynesthetes (Fig. 2E).

Across the whole range of absolute correlation thresholds of the whole cortical 2366-node network, mean weighted clustering  $(C_r)$ , a local network property, was increased in synesthetes compared with nonsynesthetes (Fig. 3A), but this difference did not reach statistical significance (p = 0.21). The mean weighted path length  $(L_r)$ , a global network property, was not statistically different between groups (p = 0.66) (Fig. 3B). In synesthetes, the small-world indices  $\gamma_r(C_r \text{ real}/C_r \text{ random})$ , a local network property compared with random networks, were reduced across the whole range of correlation thresholds compared with the networks of the nonsynesthetes (Fig. 3C), but this difference did also not reach statistical significance (p = 0.22). The small-world indices  $\lambda_r$  ( $L_r$  real/ $L_r$  random), which is a global network property compared with random networks, were not different between groups (p = 0.23) (Fig. 3D). The classical small-world scalar parameter  $\sigma$ , which is defined as  $\sigma_r = \gamma_r / \lambda_r$  and indicates the integration of local and global network characteristics, was reduced in the networks of the synesthetes compared with the networks of the nonsynesthetes (Fig. 3E), but this difference did not reach statistical significance (p = 0.20).

#### Mean degree and betweenness centrality

Mean (across nodes) degree centrality scores were significantly increased in each single 154-node network in synesthetes compared with nonsynesthetes (all p < 0.0001, Bonferroni corrected p = 0.05/16 = 0.003). When comparing the mean degree centrality scores between the groups across all nodes and networks, synesthetes showed a statistical trend toward increased degree centrality

(mean/SD, 14.76/8.36 in synesthetes and 9.99/7.00 in nonsynesthetes; p = 0.062).

With respect to the mean betweenness centrality in each single network, no significant differences were found between synesthetes and nonsynesthetes (all p > 0.027, Bonferroni corrected p = 0.05/16 = 0.003). Across the whole range of correlation thresholds and averaged across all nodes, mean betweenness centrality was not significantly different between groups (p = 0.21).

In each differently thresholded 2366-node network, mean (across nodes) degree centrality scores were significantly increased in synesthetes compared with nonsynesthetes (all  $p \ll 0.0001$ , Bonferroni corrected p = 0.05/16 = 0.003). When comparing mean degree centrality between groups (averaged across all nodes and across the differently thresholded networks), synesthetes showed significantly increased degree centrality (mean/SD, 130.3/59.9 in synesthetes and 103.5/41.2 in nonsynesthetes;  $p \ll 0.0001$ ).

With respect to mean (across nodes) betweenness centrality in each single 2366-node network, significant as well as insignificant (after Bonferroni correction) decreases were found in synesthetes compared with nonsynesthetes (0.0001  $\ll p < 0.025$ , Bonferroni corrected p = 0.05/16 = 0.003). Betweenness centrality was significantly decreased in the sparser networks and also decreased in denser networks, but the decreases in the denser networks were statistically not significant. However, averaged across all nodes and across the whole range of correlation thresholds, synesthetes showed significantly decreased mean betweenness centrality



the synesthetes (triangles) and the nonsynesthetes (squares) are shown. A, Mean weighted clustering coefficients ( $C_i$ ). B, Mean

weighted path lengths ( $L_r$ ). **C**, Weighted clustering coefficient parameters  $\gamma_r$  defined as  $C_r$  real/ $C_r$  random. **D**, Weighted path length

parameters  $\lambda_r$  defined as  $L_r$  real/ $L_r$  random. **E**, Small-world index  $\sigma_r$  defined as  $\gamma_r/\lambda_r$ . The x-axis represents the correlation

coefficient at which the association matrix was thresholded.



**Figure 3.** Whole cortical 2366-node network indices of the synesthetes and nonsynesthetes. Whole cortical network indices of the synesthetes (triangles) and the nonsynesthetes (squares) are shown. **A**, Mean weighted clustering coefficients ( $C_r$ ). **B**, Mean weighted path lengths ( $L_r$ ). **C**, Weighted clustering coefficient parameters  $\gamma_r$  defined as  $C_r$  real/ $C_r$  random. **D**, Weighted path length parameters  $\lambda_r$  defined as  $L_r$  real/ $L_r$  random. **E**, Small-world index  $\sigma_r$  defined as  $\gamma_r/\lambda_r$ . The *x*-axis represents the correlation coefficient at which the association matrix was thresholded.

(mean/SD, 1313.1/947.1 in synesthetes and 1409.6/872.9 in non-synesthetes; *p* = 0.0003).

## Identification of hub regions

Hub regions were identified by weighted mean degree and betweenness centrality scores averaged across all differently thresholded networks. The centrality scores of the 15 largest hubs and that of the FuG and IPS in the whole cortical 154node network are listed in Table 1, and all mean degree and betweeneess centralities are visualized in Figures 4 and 5, respectively.

Across the 15 largest hubs, mean degree centrality scores were significantly increased in synesthetes compared with nonsynesthetes (mean/SD, 31.3/5.3 in synesthetes and 20.7/ 6.4 in nonsynesthetes; p < 0.0001). The left FuG is one of the largest hub nodes in both groups, although its degree centrality is much higher in synesthetes than nonsynesthetes. The right FuG and both IPS are higher in the synesthetes' hub node (degree) hierarchy relative to the hierarchy of the nonsynesthetes. Mean degree centrality scores of the regions of interest averaged across all networks were as follows: left FuG, mean/SD for synesthetes and nonsynesthetes was 35.9/10.5 and 26.7/12.7 (p = 0.017); right FuG, 28.1/11.6 and 12.3/9.0 (p < 0.0001); left IPS, 15.4/8.9 and 5.7/4.9 (p = 0.0001); right IPS, 27.2/12.7 and 6.1/5.2 ( $p \ll 0.0001$ ).

With respect to betweenness centrality across the 15 largest hubs, there were no significant differences between the groups ( p = 0.21). Mean betweenness centrality scores of the FuG

and IPS averaged across all networks were as follows: left FuG, mean/SD for synesthetes and nonsynesthetes was 98.0/56.0 and 91.2/56.8 (p = 0.71); right FuG, 28.1/25.2.6 and 116.4/68.9 (p < 0.0001); left IPS, 130.8/39.6 and 332.3/245.7 (p = 0.0009); right IPS, 43.4/22.9 and 37.2/37.0 (p = 0.53).

Note that the differences in degree and betweenness centrality scores of the nodes in the FuG and IPS have a low specificity because a lot of other cortical areas (nodes) also showed statistically significant differences with respect to degree and/or betweenness centrality between synesthetes and nonsynesthetes.

The centralities scores of the 20 largest hubs in the whole cortical 2366-node network are listed in Table 2. All degree centralities and all betweenness centralities are visualized in supplemental Figs. S3 and S4 (available at www.jneurosci. org as supplemental material), respectively. Across the 20 largest hubs, mean degree centrality scores were significantly increased in synesthetes compared with nonsynesthetes (mean/SD, 308.3/18.1 in synesthetes and 228.7/8.6 in nonsynesthetes;  $p \ll 0.0001$ ). Degree centrality across all 14 left and across all 14 right fusiform nodes were statistically not significantly different between groups (p = 0.29 and p = 0.21, respectively). However, degree centrality across all 34 left intraparietal nodes was significantly increased in synesthetes

compared with nonsynesthetes (mean/SD, 183.1/48.5 in synesthetes and 116.5/33.6 in nonsynesthetes;  $p \ll 0.0001$ ), and for the 34 right-hemispheric intraparietal nodes as well (mean/SD, 156.7/51.5 in synesthetes and 89.6/30.7 in nonsynesthetes;  $p \ll 0.0001$ ).

Across the 20 largest hubs, mean betweenness centrality scores tended to be significantly increased in synesthetes compared with nonsynesthetes (mean/SD, 5466/702 in synesthetes and 5116/454 in nonsynesthetes; p = 0.070). Betweenness centrality across all 14 left and across all 14 right fusiform nodes was not statistically different between groups (p = 0.91 and p = 0.10, respectively). Betweenness centrality across all 34 left intraparietal nodes was statistically not significant different between groups (p = 0.68). However, betweenness centrality across the 34 right intraparietal nodes was significantly increased in synesthetes compared with nonsynesthetes (mean/SD, 1477/823 in synesthetes and 1040/577 in nonsynesthetes, p = 0.011).

#### Modularity analysis

Hierarchical modularity analysis of the whole cortical 154-node network revealed, on average, 10–11 clusters in both groups (mean/SD, 9.9/8.4 clusters in synesthetes and 11.0/9.52 clusters in nonsynesthetes; p = 0.73). Modularity measures (Q values) ranged from 0.141 (densest network) to 0.373 (sparsest network) in synesthetes and from 0.184 to 0.552 in nonsynesthetes. Mean modularity was significantly lower in synesthetes compared with

	Synesthetes				Nonsynesthetes				
	Rank	Node	Absolute centrality	Normalized centrality	Rank	Node	Absolute centrality	Normalized centrality	
Degree	1	r_CgS_i	42.4	0.2756	1	r_MTG	28.5	0.1851	
	2	I_IFS	36.6	0.2374	2	l_FuG	26.7	0.1732	
	3	I_FuG	35.9	0.2333	3	r_CgS_i	26.3	0.1708	
	4	r_SOG	35.3	0.2292	4	r_0FG	24.6	0.1598	
	5	I_InsG_L	32.8	0.2130	5	I_FMG	24.5	0.1592	
	6	I_TMP	32.1	0.2083	6	r_SbGG	24.1	0.1564	
	7	r_OCP	32.0	0.2079	7	r_SOG	23.3	0.1511	
	8	I_OFS_H	31.8	0.2065	8	r_ITG	22.8	0.1480	
	9	r_ITG	31.0	0.2014	9	r_Cun	22.3	0.1448	
	10	I_TTS	31.0	0.2014	10	I_IFS	22.1	0.1435	
	11	r_SPL	31.0	0.2010	11	r_InsG_L	21.6	0.1400	
	12	I_IMS_pJ	30.6	0.1988	12	I_SbPS	21.5	0.1397	
	13	r_LF_av	30.2	0.1960	13	I_OFS_H	20.7	0.1343	
	14	r_CG_I	29.9	0.1943	14	I CG M	19.7	0.1282	
	15	r_TTS	29.8	0.1933	15	r_IFG_Op	19.6	0.1270	
	19	r_FuG	28.1	0.1824	48	r_FuG	12.3	0.0797	
	22	r IPS	27.2	0.1765	108	r IPS	6.1	0.0393	
	68	I_IPS	15.4	0.1002	112	I_IPS	5.7	0.0372	
Betweenness centrality	1	l_Pcu	643.4	0.0553	1	r_POS	544.7	0.0468	
	2	r_SFG	408.8	0.0352	2	I_SFG	432.2	0.0372	
	3	r_POS	353.0	0.0304	3	I_POS	420.9	0.0362	
	4	I_SFG	298.1	0.0256	4	I_Pcu	399.1	0.0343	
	5	I_IFG_Op	286.0	0.0246	5	I_SbCG	362.2	0.0311	
	6	I_IFG_Tr	258.0	0.0222	6	I IPS	332.3	0.0286	
	7	I_AOS	255.0	0.0219	7	I_AnG	309.9	0.0266	
	8	r_CG_M	232.6	0.0200	8	I CG M	304.2	0.0262	
	9	I_InsS_Ca	207.7	0.0179	9	I_LiG	297.3	0.0256	
	10	I_MTG	207.4	0.0178	10	r_MTG	287.3	0.0247	
	11	l_LiG	195.1	0.0168	11	I_ITG	245.1	0.0211	
	12	I_AnG	190.5	0.0164	12	r_IFG_Tr	242.9	0.0209	
	13	r_Cun	185.9	0.0160	13	I_PCL	239.3	0.0206	
	14	I_PrCS_S	175.8	0.0151	14	I_SMG	238.0	0.0205	
	15	r_OTS_m	168.6	0.0145	15	I_STS	231.3	0.0199	
	28	I_IPS	130.8	0.0112	37	r_FuG	116.4	0.0100	
	45	l_FuG	98.0	0.0084	44	I_FuG	91.2	0.0078	
	74	r_IPS	43.4	0.0037	95	r_IPS	37.2	0.0032	
	94	r FuG	28.1	0.0024		—			

Shown are the 15 largest hub regions. The ranks of the left and right FuG and IPS are shown also. Note the significantly higher degree centrality scores of the 15 largest hubs in synesthetes compared with nonsynesthetes (two-sample *t* test,  $p \ll 0.0001$ ). Although nonsynesthetes showed Increased betweenness centrality scores, this difference is not statistically significant (p = 0.21). Normalized degree centrality is computed by dividing the absolute degree by the number of nodes (154) in the network. Normalized betweenness centrality scores were computed by dividing the absolute betweenness by  $[(1/2) \times (154 - 1) \times (154 - 2)]$ . The values of the FuG and IPS are printed in bold. For the code of the structural parcellation labels, see supplemental Table S2 (available at www.jneurosci.org as supplemental material).

nonsynesthetes (mean/SD, 0.223/0.072 in synesthetes and 0.319/0.115 in nonsynesthetes; p = 0.0095).

Intramodular connectivity for the right FuG was not significantly different between groups (Bonferroni corrected). However, intramodular connectivity was increased in synesthetes compared with nonsynesthetes for the left FuG (mean/SD, 0.72/0.93 in synesthetes and -0.21/0.80 in nonsynesthetes; p = 0.0053), the left IPS (mean/SD, 1.50/0.20 in synesthetes and 0.80/0.49 in nonsynesthetes; p < 0.0001), and the right IPS (mean/SD, 0.41/0.24 in synesthetes and -0.30/0.31 in nonsynesthetes;  $p \ll 0.0001$ ).

Intermodular connectivity was not significantly different between groups for both FuG and for the left IPS (all p > 0.017, Bonferroni corrected p = 0.05/4 = 0.015). For the right IPS, however, intermodular connectivity was increased in synesthetes compared with nonsynesthetes (mean/SD, 0.99856/0.0012 in synesthetes and 0.98945/0.0114 in nonsynesthetes;  $p \ll 0.0001$ ).

Note that the differences in intramodular and intermodular connectivity of the nodes in the FuG and IPS have a low specificity because a lot of other cortical areas (nodes) also showed statistically significant differences in these connectivity measures between synesthetes and nonsynesthetes. The hierarchical modularity analysis of the whole cortical 2366-node network revealed, on average, six to seven clusters in both groups (mean/SD, 6.0/2.3 clusters in synesthetes and 6.9/3.5 clusters in nonsynesthetes; p = 0.38). Modularity measures (Q values) ranged from 0.135 (densest network) to 0.367 (sparsest network) in synesthetes and from 0.142 to 0.411 in nonsynesthetes (mean/SD, 0.224/0.069 in synesthetes and 0.241/0.081 in nonsynesthetes; p = 0.53).

When focusing on intramodular connectivity (normalized within-module degree) of the FuG and IPS nodes, there were no significant differences between synesthetes and nonsynesthetes for both FuG and for the left IPS (all p > 0.50). The synesthetes' right IPS, however, showed significantly increased intramodular connectivity (z-score; mean/SD, 0.32/0.83 in synesthetes and -0.43/0.51 in nonsynesthetes; p < 0.0001).

With respect to intermodular connectivity (participation coefficient), there was no significant difference for the left and right FuG nodes between the groups (p = 0.82 and p = 0.24, respectively). For the left IPS, intermodular connectivity was increased in synesthetes compared with nonsynesthetes (participation coefficient; mean/SD, 0.99972/0.0006 in synesthetes and 0.99908/ 0.0011 in nonsynesthetes; p = 0.006), and for the right IPS as well



**Figure 4.** Weighted degree centrality of the nodes in the whole cortical 154-node network of the synesthetes and nonsynesthetes. Weighted degree centrality scores averaged across all networks (correlation thresholds) for the synesthetes (top) and the non-synesthetes (bottom) are shown. Note that the size of the spheres represents the weighted degree centrality scores; the black lines represent the edges (connections) between the nodes, and the different colors represent the nodes within the different lobes (blue, frontal; pink, limbic; yellow, temporal; orange, temporo-occipital; red, occipital; green, parieta; light green, parieto-frontal). IFuG, rFuG, Left and right fusiform gyrus; IIPS, rIPS, left and right intraparietal sulcus.

(mean/SD, 0.99943/0.0008 in synesthetes and 0.99783/0.0031 in nonsynesthetes; p = 0.005).

#### Fusiform-lingual 132-node network analysis

The main results of the present study are based on the whole cortical 2366-node and 154-node network. We did perform an additional analysis on the fusiform-lingual network. This 132-node network was constructed in isolation from other cortical areas outside the fusiform-lingual complex, except its directly adjacent areas. This analysis showed no significant differences between synesthetes and nonsynesthetes in clustering, path length, gamma, lambda, and sigma (see supplemental Results and supplemental Fig. S5, available at www.jneurosci.org as supplemental material).

Mean degree and betweenness centrality across all nodes and networks were not significantly different between the groups. However, mean degree centrality averaged across the 18 left FuG nodes was significantly decreased in synesthetes (mean/SD, 7.5/ 3.3 in synesthetes and 10.2/4.2 in nonsynesthetes; p = 0.034). Mean degree centrality averaged across the 17 right FuG nodes was also significantly decreased in synesthetes (mean/SD 8.7/ 3.0 in synesthetes and 12.4/2.6 in nonsynesthetes; p = 0.0005). There were no significant differences between synesthetes and



**Figure 5.** Weighted betweenness centrality of the nodes in the whole cortical 154-node network of the synesthetes and nonsynesthetes. Weighted betweenness centrality scores averaged across all networks (correlation thresholds) for the synesthetes (top) and the nonsynesthetes (bottom) are shown. Note that the size of the nodes represents the weighted betweenness centrality scores; the black lines represent the edges (connections) between the nodes, and the different colors represent the nodes within the different lobes (blue, frontal; pink, limbic; yellow, temporal; orange, temporo-occipital; red, occipital; green, parietal; light green, parieto-frontal). IFuG, rFuG, Left and right fusiform gyrus; IIPS, rIPS, left and right intraparietal sulcus.

nonsynesthetes in betweenness centrality. Please note that degree and betweenness centrality within the fusiform-lingual 132-node network was based only on edges (connections) within the fusiform-lingual complex and its adjacent cortical areas, meaning that all edges to other cortical areas located outside of the fusiform-lingual complex and its adjacent cortical areas were excluded.

The direction of the effects (and their statistical significance) of the different network parameters, the network efficiency, and the shifts toward a more regular or random network configuration of the whole cortical 2366-node, whole cortical 154-node, and fusiform-lingual 132-node networks are summarized in Table 3.

## Discussion

MRI surface-based morphometry and graph theoretical network analysis revealed small-worldness of structural brain networks of both grapheme-color synesthetes and nonsynesthetes. This is because networks had an almost identical path length ( $\lambda_r \approx 1$ ) (Fig. 2D,3D) but were more locally clustered ( $\gamma_r > 1$ ) (Figs. 2C, 3C) compared with matched random networks, and this finding is consistent with network analyses of data derived from cortical thickness correlations as well as diffusion tensor and spectrum imaging-based fiber tractogra-

Table 2. Hub regions in the whole cortical 2366-node network revealed <b>b</b>	oy weig	ghted d	legree and	l betweenness co	entrality
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	Synesthetes				Nonsynesthetes				
	Rank	Node	Absolute centrality	Normalized centrality	Rank	Node	Absolute centrality	Normalized centrality	
Degree centrality	1	I_SMG div. 13	356.1	0.1505	1	r_POS div. 6	249.3	0.1054	
	2	I_SMG div. 14	348.6	0.1473	2	I_SFG div. 5	236.6	0.1000	
	3	I_SMG div. 12	323.3	0.1366	3	r_POS div. 12	236.3	0.0999	
	4	I_Pcu div. 15	319.1	0.1349	4	r_POS div. 10	236.1	0.0998	
	5	r_PCL div. 12	316.3	0.1337	5	r_CS div. 10	235.8	0.0996	
	6	I_Pcu div. 16	313.1	0.1323	6	r_POS div. 9	235.2	0.0994	
	7	I_PrCG div. 27	312.5	0.1321	7	I_SbCG div. 10	234.9	0.0993	
	8	SOS div. 3	309.6	0.1309	8	r_SMG div. 21	234.1	0.0989	
	9	I SFG div. 14	306.5	0.1295	9	AnG div. 15	230.2	0.0973	
	10	PrCG div. 23	306.4	0.1295	10	I ITG div. 2	230.0	0.0972	
	11	MOG div. 14	301.9	0.1276	11	AnG div. 14	227.8	0.0963	
	12	PrCG div. 26	300.8	0.1272	12	r POS div. 11	225.5	0.0953	
	13	r PCL div. 10	300.4	0.1269	13	POS div. 12	223.7	0.0945	
	14	r PoCS div. 2	296.2	0.1252	14	Pcun div. 17	223.7	0.0945	
	15	r CG M div. 6	296.1	0.1252	15	r SMG div. 20	223.0	0.0942	
	16	I IFG Tr div. 7	295.7	0.1250	16	r SMG div. 19	219.5	0.0928	
	17	PrCG div. 21	293.2	0.1239	17	PCS div. 11	219.1	0.0926	
	18	I SPL div. 20	290.5	0.1228	18	r SOG div. 10	217.9	0.0921	
	19	PrCG div. 22	289.6	0.1224	19	r OTS m div. 9	217.8	0.0920	
	20	I PCL div. 15	289.4	0.1223	20	I SPL div. 21	217.3	0.0918	
Betweenness centrality	1	I SMG div. 13	8050.9	0.0029	1	r POS div. 6	6090.8	0.0022	
,	2	L (S div. 30	6048.4	0.0022	2	I ITG div. 2	5900.9	0.0021	
	3	L SOS div. 3	5956.1	0.0021	3	r_SMG div. 19	5783.9	0.0021	
	4	r PCL div. 10	5954.9	0.0021	4	L AnG div. 15	5739.1	0.0021	
	5	r TTG div. 2	5736.6	0.0021	5	r CS div. 10	5519.2	0.0020	
	6	PrCG div. 26	5592.5	0.0020	6	I Prun div. 17	5286.1	0.0019	
	7	PrCG div. 23	5382.0	0.0019	7	PoCG div. 1	5147.1	0.0018	
	8	I Pr(G div 27	5339.9	0.0019	8	L MOG div 14	5131 1	0.0018	
	9	L OTS Ldiv. 1	5294.8	0.0019	9	r_SMG div. 21	5071.6	0.0018	
	10	L PoCS div. 28	5291.8	0.0019	10	r POS div. 8	4937.1	0.0018	
	11	r PCL div 12	5245 1	0.0019	11	r (G M div 3	4892.2	0.0018	
	12	L SFG div. 14	5173.1	0.0019	12	L SOG div. 1	4887.3	0.0017	
	13	L AOS div. 2	5117.3	0.0018	13	L ITG div. 3	4879.3	0.0017	
	14	L MOG div 14	5091 9	0.0018	14	r SMG div 20	4853 5	0.0017	
	15	L SMG div. 17	5081.1	0.0018	15	L IFS div 5	4772 8	0.0017	
	16	I_SMG div. 12	5069.0	0.0018	16	r IFS div 10	4747 1	0.0017	
	17	Pr(G div 22	5060 2	0.0018	17	L POS div 9	4720.2	0.0017	
	18	L STS div 15	5025 1	0.0018	18	r ShCG div 8	4675 4	0.0017	
	19	r PoCS div 2	4907 9	0.0018	19	L ShCG div. 0	4646 9	0.0017	
	20	I IFG Tr div. 7	4905.6	0.0018	20	I SMG div. 14	4628.9	0.0017	

Shown are the 20 largest hub regions. Note the significantly higher degree centrality scores of the 20 largest hubs in synesthetes compared with nonsynesthetes (two-sample *t* test,  $p \ll 0.0001$ ). Although synesthetes showed Increased betweenness centrality, this difference shows only a statistical trend toward significance (p = 0.069). Normalized degree centrality is computed by dividing the absolute degree by the number of nodes (2366) in the network. Normalized betweenness centrality is computed by dividing the absolute betweenness by  $[(1/2) \times (2366 - 1) \times (2366 - 2)]$ . For the code of the structural parcellation labels, see supplemental Table S2 (available at www.jneurosci.org as supplemental material). div., Division.

phy in normal and clinical samples (He et al., 2007, 2008, 2009; Bassett et al., 2008; Chen et al., 2008; Hagmann et al., 2008; Gong et al., 2009; Li et al., 2009).

## Analysis based on the whole cortical 154-node and 2366-node network

We report first evidence of differences in topological characteristics of structural brain networks across the entire cortex between synesthetes and nonsynesthetes. Clustering coefficients were significantly increased in the synesthete's brain indicating higher local hyperconnectivity (cliquishness) of cortical areas in GCS, suggesting an increased capability in local information processing and integration as well as a shift of the synesthetes' network topology toward a more regular configuration. Path lengths tended to be shorter in synesthetes, suggesting increased network efficiency (i.e., faster global information propagation).

In comparison of the real network with 100 random networks, the  $\gamma_r$  ratio ( $C_r$  real/ $C_r$  random) was significantly reduced in synesthetes compared with nonsynesthetes, suggesting that the network of the former is shifted toward a more random configuration compared with that of the latter. A more random network configuration is associated with increased efficiency in global information propagation.

By integrating the clustering coefficient (a local network property) and the path length (a global network property) relative to random networks into the measure of smallworldness,  $\sigma_r = \gamma_r / \lambda_r$ , it is evident that small-world properties are significantly reduced in grapheme-color synesthetes. This indicates that the topological network organization (connectivity architecture) in synesthetes deviates strongly from that found in nonsynesthetes whereby increased clustering of the synesthetes' networks is the predominant feature of their reduced small-world architecture. Note that although clustering was increased in synesthetes' networks, it is actually lower than what would be expected in an equivalent network with a random configuration, and therefore these networks, in fact, have reduced small-worldness compared with nonsynesthetes.

## Table 3. Summary of the direction of effects, statistical significance, network efficiency, and shifts in network configuration toward a more regular or random organization

				Network efficiency		Shift in configuration		
	Network measure	Direction of effects	Statistical significance (p)	Global	Local	Regular	r Random	
Whole cortical 2366-node network	Clustering coefficient ( $C_r$ )	Inc. in syn	0.21		Increased	In syn		
	Path lengths $(L_r)$	Dec. in syn	0.66	Increased		,	In syn	
	Gamma (C, real/C, random)	Dec. in syn	0.22	Increased			ln syn	
	Lambda (L, real/L, random)	No effect	0.23	Similar	Similar	No shift	No shift	
	Sigma (gamma/lambda)	Dec. in syn	0.20		Increased	In syn		
	Degree across nodes and networks	Inc. in syn***	$1.7  imes 10^{-70}$		Increased			
	Betweenness across nodes and networks	Dec. in syn***	0.0003	Decreased				
	Degree left FuG	Inc. in syn	0.29		Increased			
	Degree right FuG	Inc. in syn	0.21		Increased			
	Betweenness left FuG	Inc. in syn	0.91		Increased			
	Betweenness right FuG	Dec. in syn	0.10		Decreased			
	Degree left IPS	Inc. in syn***	$1.6  imes 10^{-8}$		Increased			
	Degree right IPS	Inc. in syn***	$9.2  imes 10^{-9}$		Increased			
	Betweenness left IPS	Inc. in syn	0.68		Increased			
	Betweenness right IPS	Inc. in syn <sup>Bonf.</sup>	0.011		Increased			
Whole cortical 154-node network	Clustering coefficient (C,)	Inc. in syn***	0.001		Increased	In syn		
	Path lengths $(L_r)$	Dec. in syn**	0.001	Increased			In syn	
	Gamma (C, real/C, random)	Dec. in syn*	0.011	Increased			ln syn	
	Lambda ( $L_r$ real/ $L_r$ random)	Inc. in syn	0.17		Increased	In syn		
	Sigma (gamma/lambda)	Dec. in syn**	0.003		Increased	ln syn		
	Degree across nodes and networks	Inc. in syn	0.062		Increased			
	Betweenness across nodes and networks	Dec. in syn	0.21	Decreased				
	Degree left FuG	Inc. in syn <sup>Bonf.</sup>	0.017		Increased			
	Degree right FuG	Inc. in syn***	$2.3  imes 10^{-5}$		Increased			
	Betweenness left FuG	Inc. in syn	0.71	Increased				
	Betweenness right FuG	Dec. in syn***	$4.0  imes 10^{-6}$	Decreased				
	Degree left IPS	Inc. in syn***	0.0001		Increased			
	Degree right IPS	Inc. in syn***	$3.8  imes 10^{-8}$		Increased			
	Betweenness left IPS	Dec. in syn***	0.0009	Decreased				
Fusiform-lingual 132-node network	Clustering coefficient (C <sub>r</sub> )	No effect	0.69	Similar	Similar	No shift	No shift	
	Path lengths $(L_r)$	No effect	0.68	Similar	Similar	No shift	No shift	
	Gamma (C, real/C, random)	No effect	0.73	Similar	Similar	No shift	No shift	
	Lambda (L, real/L, random)	No effect	0.82	Similar	Similar	No shift	No shift	
	Sigma (gamma/lambda)	No effect	0.70	Similar	Similar	No shift	No shift	
	Degree across nodes and networks	No effect	0.23	Similar	Similar			
	Betweenness across nodes and networks	No effect	0.82	Similar	Similar			
	Degree left fusiform subregions	Dec. in syn*	0.034		Decreased			
	Degree right fusiform subregions	Dec. in syn***	0.0005		Decreased			
	Betweenness left fusiform subregions	Inc. in syn	0.70		Increased			
	Betweenness right fusiform subregions	Inc. in syn	0.13		Increased			

These measures are shown for the whole cortical 2366-node network (top third), the whole cortical 154-node network (middle third), and the fusiform-lingual 132-node network (bottom third). Note that shifts in network configuration toward a more regular or random configuration are relative to the other group. Dec., Decreased; Inc., Increased; *r*, correlation threshold; syn, synesthetes; \*p < 0.05; \*\*p < 0.01; \*\*\*p < 0.001; Bonf., not statistically significant after Bonferroni correction.

"Small worlds" are attractive models for the description of complex brain networks because they support both local segregated and integrated information processing (Sporns et al., 2004) and minimize the brain's wiring costs while simultaneously maximizing the efficiency of global information propagation (Kaiser and Hilgetag, 2006; Achard and Bullmore, 2007). Since small-world networks reflect an optimal balance between local processing specialization/integration and global information propagation, higher clustering in the synesthetes' networks indicates a disruption of this normal balance. Regular lattices have been suggested as reducing global signal propagation speed and synchronisability compared with small-world networks (Strogatz, 2001). We do not consider synesthesia to be a disorder, but, as far as clustering is concerned, an altered network architecture similar to that found in the present study for grapheme-color synesthetes was found in patients with Alzheimer's disease (AD) (He et al., 2008), although these AD patients showed slightly longer path lengths rather than slightly shorter path lengths as synesthetes. This pattern of topological organiza-

tion leads to an increase in local network efficiency, but a decrease in global efficiency compared with elderly control subjects, suggesting a more regular network configuration in AD (He et al., 2008). This is in contrast to the reduced local network efficiency reported in multiple sclerosis (He et al., 2009). In our synesthetes, local network efficiency is enhanced, as indicated by increased clustering and reduced gamma and sigma. These GCS-related changes in small-world characteristics might be considered as reflecting a less optimal topological network organization characterized by increased clustering and reduced small-worldness. This has implications for the understanding of the relationship between brain network topological characteristics and the evolution of the synesthetic experience of graphemes in GCS. Together, these results suggest that hyperconnectivity in synesthetes is global and not restricted to the FuG and IPS as implied by the current synesthesia literature.

The results of the centrality measurement analyses were in accordance with the findings of the small-world analysis. Mean (across nodes and networks) degree centrality was significantly increased in synesthetes compared with nonsynesthetes. Within the whole cortical 154-node network, both FuG and IPS revealed higher-degree centrality in the networks of the synesthetes. In the whole cortical 2366-node networks, the FuG and IPS nodes showed increased degree centrality scores in synesthetes, but only degree centrality of the IPS nodes were significantly different between groups. Indeed, this suggests that the IPS (and FuG) is globally hyperconnected with other nodes in the synesthete's network. However, this finding has a low specificity because a lot of other nodes (42 of 154) in the 154-node network of the synesthetes showed also significant differences in degree centrality scores: 37 of these 42 nodes showed increased centrality in synesthetes. A similar low specificity of increased FuG and IPS degree centrality was also found for the 2366-node network. The findings in degree centrality support the notion that topological alterations in the network of the synesthetes are widespread and go beyond the FuG and IPS. Other nodes with increased degree centrality in the whole cortical 154-node network were located in the right planum polare, left superior temporal sulcus, left temporal pole, left pars triangularis, right Heschl's sulcus, left precuneus, and regions of the right insula. It is interesting to note that most of these high-degree centrality nodes in the whole cortical 154-node network can be associated with auditory processing, and it has been recently reported that some of these areas are also involved in GCS (Rouw and Scholte, 2010).

The hierarchical modularity analysis of the whole cortical 2366-node and 154-node networks revealed increased intramodular and also intermodular connectivity of the IPS in the synesthetes' brain. However, modularity of structural brain networks was significantly reduced in the whole cortical 154-node networks of synesthetes compared with nonsynesthetes, suggesting a reduced modular brain organization in GCS, which might have functional consequences.

## Analysis based on the fusiform-lingual 132-node network

When looking for hyperconnectivity of the FuG within the fusiform-lingual 132-node network, no significant differences in network architecture were found between synesthetes and nonsynesthetes. Neither the clustering coefficients and path lengths nor the small-world indices and betweenness centrality scores were significantly different between synesthetes and nonsynesthetes. Unexpectedly, mean degree centrality of fusiform subregions was significantly decreased in synesthetes compared with nonsynesthetes, suggesting hypoconnectivity within the ventral visual stream but simultaneously suggesting hyperconnectivity of the FuG nodes to areas outside of the fusiform-lingual complex. This is further evidence for a global instead of a local hyperconnectivity in GCS. Our finding derived from the analysis of the fusiform-lingual 132-node network is not compatible with the idea that GCS originates from hyperconnectivity between visual word form areas and the color processing areas, which are both located on the FuG (Hubbard and Ramachandran, 2005; Hubbard, 2007).

## Is GCS not the only phenotype?

We suggest that synesthetic experiences might be only one phenotypic manifestation of the reduced small-world architecture in synesthetes. Such an interpretation has already been proposed by Bargary and Mitchell (2008). Widespread differences in the topological organization of white matter connectivity within the synesthetic brain as well as the low modularity of the synesthetes' connectivity architecture are compatible with reports of other phenotypic manifestations in synesthetes, including possible differences in creativity (Ward et al., 2008), mental imagery (Barnett and Newell, 2008), and higher incidence of "Mitempfindung" (the referral of a tactile sensation to a location far away from the stimulation site) (Burrack et al., 2006). Furthermore, some synesthetes have an extraordinary autobiographical memory capacity (Parker et al., 2006), and time–space synesthetes show enhanced performance in temporal and visuospatial tasks (Simner et al., 2009).

Whether the reduced small-world organization of structural brain network in synesthetes is caused by a failure in neural pruning (Kennedy et al., 1997; Rodman and Moore, 1997) or even by synaptic sprouting (Armel and Ramachandran, 1999) remains to be shown in future investigations. Several methodological considerations of the present study, including differences in results between the 154-node and 2366-node networks, are addressed in the supplemental Discussion (available at www.jneurosci.org as supplemental material).

## Conclusions

The present findings reveal reduced small-world topology of structural brain networks in grapheme-color synesthetes. Reduced small-worldness in GCS is driven by increased clustering, suggesting that the synesthete's brain as a whole is strongly hyperconnected. This altered pattern of connectivity indicates a disruption of the normal interplay between local information integration and global information propagation and is associated with increased local network processing efficiency. We concluded that hyperconnectivity is not restricted to the FuG and IPS, implying that synesthetic experiences might be only one phenotypic manifestation of the reduced small-world architecture in synesthetes. Although our findings provide strong evidence for a globally hyperconnected brain architecture in synesthetes, we cannot entirely rule out the proposed pivotal role of the FuG and IPS in GCS.

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